GA and Tabu Search Chae Y. Lee

# **Changing Representation During Search: Delta Coding**

### Introduction

- **Remapping** strategy to focus search around good solutions that have already been discovered either by initial GA or by delta coded GA
- The best solution parameters are saved as the *interim solution* and the GA is restarted with a new random population
- Parameter substrings are decoded such that they represent a distance or *delta value*  $(\pm \delta)$  away from the interim solution parameters: a new hypercube is formed with the interim solution at its origin
- Delta coding sustains search by periodically **reinitializing** the population, thereby avoiding less and less population diversity: reduces and enlarges the size of hypercube currently being searched

## Delta Coding Algorithm

Delta coding uses GENITOR as the basic engine for GA

- Each parameter, when decoded for fitness evaluation, is applied as a delta value  $(\pm \delta)$  to the interim solution saved from the previous iteration
- **Remapping** (numeric shift) is performed using the 1<sup>st</sup> bit in each parameter as a sign bit and remaining bits as the delta value (Table 1)
- This remapping method (by delta coding) of applying the new strings to the interim solution searches a new hypercube with the interim solution at its origin (Figure 2)
- Thus avoiding local optima and converging on the global optimum (Figure 3)
- The process of selection, crossover and inserting offspring continues

#### GA and Tabu Search Chae Y. Lee Delta Coding Algorithm - Remapping

Table 1. Delta coding numeric shift (remapping) example.

numeric parameters	0	1	2	3	4	5	6	7
binary coding	000	001	010	011	100	101	110	111
numeric shifts	0	1	2 -	3	-3	-2	-1	-0
simple delta coding	000	001	010	011(	111	110	101	100



Figure 2. Points sampled in a one-dimensional numeric space using delta coding.

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Figure 3. Remapping search space with delta coding; interim solution 0000. Figure (b) includes the delta encoding (row 1) and the original encoding (row 2).

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- At the end of each delta iteration, the size of the hypercube is changed by altering the parameter length: **reinitialization**
- If the new best solution is different from the previous interim solution, the number of bits used to encode each delta value  $(\pm \delta)$  is reduced by one bit: this shrinks the hypercube and focuses the search in subpartitions that appear promising (Figure 4)
- When a delta iteration converges to exactly the same solution, the number of bits used is increased by one bit: this expands the hypercube and allows the GA to search a larger partition of the search space (Figure 5)



Figure 4. Crawling along a rough fitness surface. Assuming the search has converged to the interim solution at point 1, the subpartition of hyperspace defined by window 1 is searched. This allows the search to converge to point 2. The subpartition of hyperspace surrounding point 2 is then searched, converging on point 3. The search eventually converges on point 5.



reinitialization

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Figure 5. Expanding the delta coding search window after converging to the same interim solution on consecutive iterations using a reduced search space string representation.

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### De Jong Function Test Bed

